# <u>ST ANNE'S</u> NUMERACY BOOKLET



'Numeracy is the ability to understand and work with numbers' This booklet has been produced to give parents/carers and pupils' guidance on how certain common Numeracy topics are taught throughout the school.

"St Anne's is committed to raising the standards of Numeracy of all its students. We want all our pupils to be confident and capable in the use of Numeracy to support their learning in all areas of the curriculum and to acquire the skills necessary to help achieve success in Further and Higher education, employment and adult life"

# INTRODUCTION

### Purpose of this booklet is:

- To develop, maintain and improve standards in Numeracy across our school
- ✓ To ensure consistency of methods and vocabulary used across subject areas
- ✓ To help pupils recognise the skills they need for their work which will ensure consistency in the methods they will need to use

At St Anne's, we intend that all of our pupils should:

- ✓ Be able to read and write numbers AND be able to order numbers in terms of size
- ✓ Be able to recall their times tables up to at least 12
- ✓ Be able to develop their skills in estimating and approximation and have strategies to check that their answers make sense
- ✓ Be able to explain their method and reasoning using consistent language and mathematical notation
- Be able to interpret, explain and make predictions from tables, graphs and charts
- ✓ Be able to measure using suitable units and be able to convert between various units
- ✓ Be able to read from a range of meters, dials and scales
- Be able to apply an appropriate method to help solve a problem using a mental or written method

Numeracy Across St Anne's

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### WHAT NUMERACY LOOKS LIKE IN OTHER SUBJECTS

Here are some examples:

ART - Symmetry, use of paint mixing as a ratio, Scale

**ENGLISH** - comparison of texts & characters using tables or Venn diagrams

FOOD TECHNOLOGY - recipes in a ratio context, reading scales, time

DESIGN TECHNOLOGY - measuring, ratio, area & volume

**GEOGRAPHY** - representing data and interpreting data, scale ratios

**HISTORY** - timelines, sequencing events

**ICT** - representing data, spreadsheets, formulae

**MFL** - Dates, sequences and counting in other languages, use of basic graphs and surveys to practise foreign language vocabulary and reinforce interpretation of data

**MUSIC** - Counting beats, fraction bars

**PE** - Measuring & recording data, time-keeping, scoring, using percentages

**RELIGIOUS STUDIES**- Timelines, use of charts and graphs to make comparisons

**SCIENCE** - Measuring, recording and interpreting data, Units, Ratio & Percentages, Decimal & Fractions, Standard Form, Averages, Tables & Charts, Averages, 2D & 3D shapes, Area & Volume, Algebra Notation, Formulae, Equations

#### READING AND WRITING NUMBERS

You may find large numbers written with commas or spaces – both are correct. If you use commas, remember to work from the **end** of the number and place a comma **every three digits:** 

Example: **3574** is written as **3,574** or **3 574** (Three thousand five hundred and seventy four)

**48600** is written as **48,600** or **48 600** (Forty eight thousand six hundred)

REMEMBER: THE FINAL THREE DIGITS ARE READ AS THEY ARE WRITTEN IN THE ORDER  $\rightarrow$ HUNDREDS, TENS and UNITS

Tor larger numbers (remember the place values below)								
Millions	Hundred	Ten	Thousands	Hundreds	Tens	Units		
	Thousands	Thousand						
7	5	3	2	1	8	9		

Writing this out gives us (remember to start from the end and insert a comma every three digits)

• 7532189 which written with commas is 7, 532, 189

For larger numbers (nemember the place values below)

This number reads as seven **million**, five hundred and thirty two **thousand**, one **hundred a**nd eighty nine.

Millions	Hundred	Ten	Thousands	Hundreds	Tens	Units
	Thousands	Thousand				
		6	2	4	3	1

• 62, 431 is read as sixty two thousand four hundred and thirty one

More examples:

- 564, 301 is read as five hundred and sixty four thousand three hundred and one
- 3,074,200 is read as three million seventy four thousand two hundred
- 9, 268 is read as nine thousand two hundred and sixty eight
- 52, 187, 245 read as fifty two **million** one hundred and eighty seven **thousand** two **hundred** and forty five

#### ROUNDING AND ESTIMATING

<u>To the nearest 10</u>: look at the last digit, if it is less than 5 round down, if it is more than 5 then round up to the next ten. For example: 642 to the nearest ten is 640 3,479 to the nearest ten is 3,480

<u>To the nearest 100</u>: look at the last two digits, if they are less than 50 round down, if more than 50 round up For example: 3,847 to the nearest 100 is 3,800 49,362 to the nearest 100 is 49,400

<u>To the nearest 1000:</u> look at the last three digits, if they are less than 500 round down, if more than 500 round up For example: 4,213 to the nearest 1000 is 4000 283, 503 to the nearest 1000 is 284, 000

Which rounding should I choose to do a rough estimate?

- If you have a 2 digit number then round to the nearest ten
- If you have a 3 digit number then round to the nearest ten or hundred
- If you have a 4 digit number then round to the nearest hundred or thousand

<u>Example</u> Tickets for a musical show were sold over 4 days. The number of tickets sold each day was recorded in the table below. How many tickets were sold in total?

Monday	Tuesday	Wednesday	Thursday
387	208	191	312

All 3 digit numbers so round to the nearest hundred to get a rough mental estimate Estimate = 400 + 200 + 200 + 300 = 1100

```
Actual 387+208+191+312 = 1098 Good estimate!
```

**Example**: A packet of crisps weighs 72 grams. There are 19 packets in a bag. What is the total weight of the bag? (Estimate by rounding to the nearest 10) Estimate =  $70 \times 20 = 1400g$ 

Actual 72 x 19 = 1368g Good estimate!

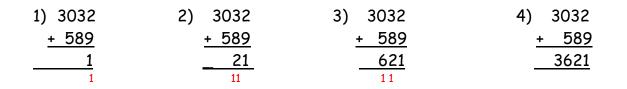
### Mental strategies ADDITION 52 There are a number of useful mental strategies for addition. Some examples are given below. \*Note: 63= 60+3 and 39=30+9 Example Calculate 63 + 39 Method 1 Add tens, then add units, then add together 60 + 30 = 903 + 9= 12 90 + 12 = 102 Method 2 Split up number to be added into tens and units and add separately. 63 + 30 = 93 93 + 9 = 102 Round up the number **being added** to the nearest 10, then subtract Method 3

63 + 40 = 103 but 40 is 1 too much so subtract 1; 103 -1 = 102

### Written Method

When adding numbers, ensure that the numbers are lined up according to place value. Start at end of the numbers and add, write down units, carry tens.

Example Add 3032 and 589





# SUBTRACTION

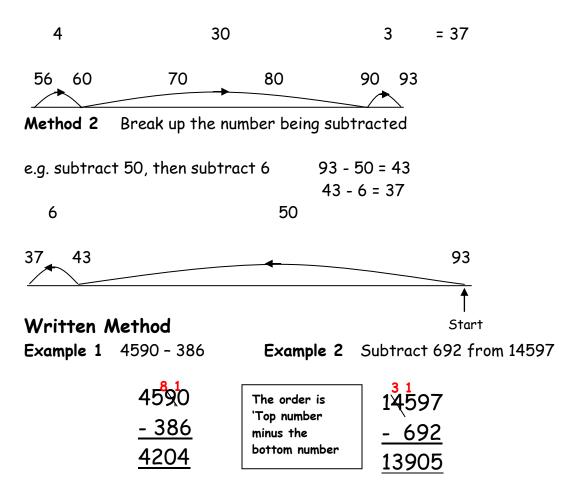


We use decomposition as a written method for subtraction (see below). Alternative methods may be used for mental calculations.

### **Mental Strategies**

- Example Calculate 93 56
- Method 1 Count on

Count on from 56 until you reach 93. This can be done in several ways e.g.



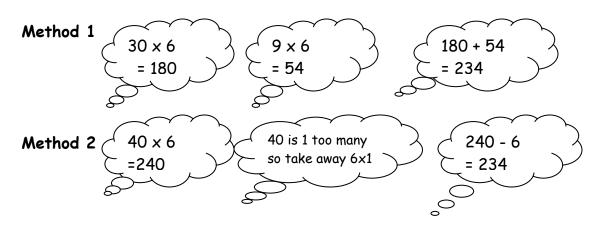
### MULTIPLICATION OF WHOLE NUMBERS (Mental)

It is essential that you know all of the multiplication tables up to 12. These are shown in the tables square below.

					_				-			
×	1	2	3	4	5	6	7	8	9	10	11	12
1	1	2	3	4	5	6	7	8	9	10	11	12
2	2	4	6	8	10	12	14	16	18	20	22	24
3	3	6	9	12	15	18	21	24	27	30	33	36
4	4	8	12	16	20	24	28	32	36	40	44	48
5	5	10	15	20	25	30	35	40	45	50	55	60
6	6	12	18	24	30	36	42	48	54	60	66	72
7	7	14	21	28	35	42	49	56	63	70	77	84
8	8	16	24	32	40	48	56	64	72	80	88	96
9	9	18	27	36	45	54	63	72	81	90	99	108
10	10	20	30	40	50	60	70	80	90	100	110	120
11	11	22	33	44	55	66	77	88	99	110	121	132
12	12	24	36	48	60	72	84	96	108	120	132	144

### Mental Strategies

Example Find 39 x 6



### MULTIPLICATION (Written Methods)

### Written strategies

### Traditional method

$$\begin{array}{r}
2 4 5 \\
\underline{x \ 6 3} \\
\hline 7_1 3_1 5 \\
\hline 14_2 7_3 0 0 \\
\hline 15 4 3 5 \end{array}$$

$$\begin{array}{r}
245 \times 3 \\
245 \times 60 \\
\hline 245 \times 60 \\
\hline 15 4 3 5 \\
\end{array}$$

### Grid method:

### **Example:** 245 x 63

X	200	40	5	
				Total
60	12000	2400	300	14700
3	600	120	15	735
Total	12600	2520	315	15435

Break down each number 245=200 +40+5 and 63=60+3

Remember: If there are 3 zeroes altogether in the calculation then there will be 3 zeroes in the answer. If there are 2 zeroes then the answer will have 2 zeroes and so on....... • Eq. 20 x 30 = 600 (do 2x3 then

**Example:** 256 X 34

256	256	7680
<u>x 30</u>	$\underline{x 4} \rightarrow$	+ <u>1024</u>
<u>7680</u>	<u>1024</u>	<u>8704</u>

Eg 20 x 30 = 600 (do 2x3 then add 2 zeroes at the end)
 400 x 20 = 8000

# DIVISION

Remember: The number you are dividing by goes outside the 'bus shelter' so for 245 ÷5 the 5 goes outside and 245 is placed inside



**Example 1** There are 192 pupils in first year, shared equally between 8 classes. How many pupils are in each class?

Example 2 Divide 4.74 by 3

$$\begin{array}{c} 1 . 5 8 \\ 4 . {}^{1}7{}^{2}4 \end{array}$$

When dividing a decimal number by a whole number, the decimal points must stay in line.

**Example 3** A jug contains 2.2 litres of juice. If it is poured evenly into 8 glasses, how much juice is in each glass?

Each glass contains 0.275 litres

If you have a remainder at the end of a calculation, add a zero onto the end of the decimal and continue with the calculation.

# ORDER OF CALCULATION (BIDMAS)

Consider this: What is the answer to  $2 + 5 \times 8$ ?

Is it 7 x 8 = 56 or 2 + 40 = 42

The correct answer is 42.



Calculations which have more than one operation need to be done in a particular order. The order can be remembered by using the mnemonic **BIDMAS** 

The **BIDMAS** rule tells us which operations should be done first. **BIDMAS** represents:

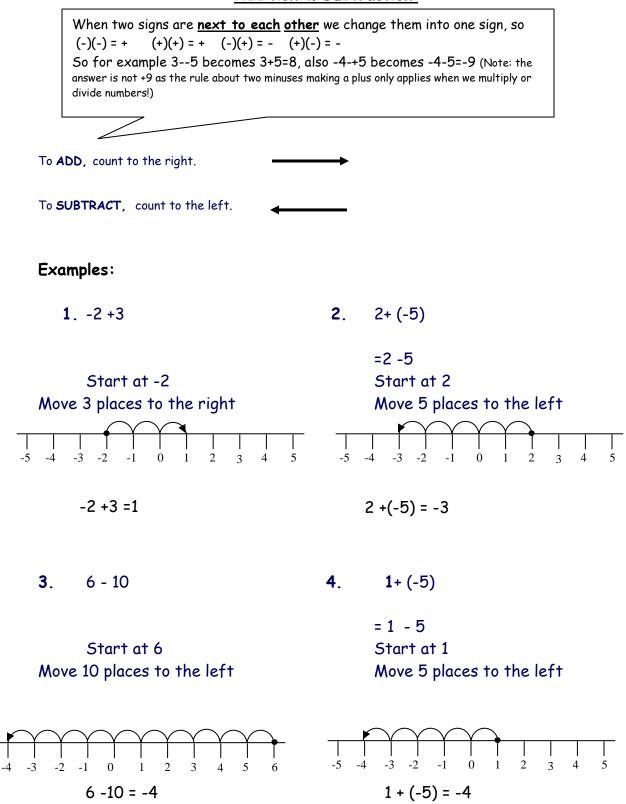
(B)rackets
(I)ndices (meaning powers like 3<sup>2</sup> or 2<sup>5</sup>)
(D)ivide
(M)ultiply
(A)dd
(S)ubract

Scientific calculators use this rule, some basic calculators may not, so take care in their use.

Example 1	15 - 12 ÷ 4 = 15 - 3 = 12	BIDMAS tells us to divide first
Example 2	(8 + 5) × 6 = 13 × 6 = 78	BIDMAS tells us to work out the brackets first
Example 3	19 + 6 ÷ (5 - 3 ) = 19 + 6 ÷ 2 = 19 + 3 = 22	

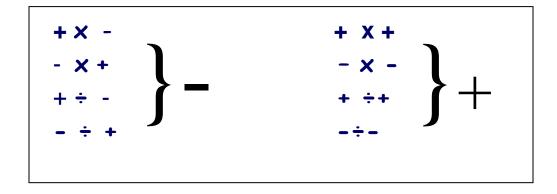
### ADDING AND SUBTRACTING NEGATIVE NUMBERS

#### Addition & Subtraction:



### MULTIPLYING AND DIVIDING NEGATIVE NUMBERS

When the signs are <u>different</u> the answer is <u>negative</u> and when the signs are the <u>same</u> the answer is <u>positive</u>:



Calculate:	Solution:
<b>a)</b> 5 × - 3	<ul> <li>a) We have +5 and -3. The signs are different, so the answer will be negative. So, 5 × -3 = -15</li> </ul>
<b>b)</b> -24 ÷ -8	<ul> <li>b) We have -24 and -8. The signs are the same, so the answer will be positive. So, -24 ÷ -8 = +3</li> </ul>
c) -6 x -2	C) We have -6 and -2. The signs are the same, so the answer will be positive. So, -6x-2=+12
d) -35 ÷ 7	<ul> <li>d) We have -35 and 7. The signs are different, so the answer will be negative. So -35 ÷ 7 = -5</li> </ul>

# FRACTIONS

### **Simplifying Fractions**

Equivalent fractions can be simplified as shown below:

The top of a fraction is called the <u>numerator</u>, the bottom is called the <u>denominator</u>. To simplify a fraction, divide the numerator and **denominator** of the fraction by the same number. Example 1 (a) ÷5 ÷8 (b) 20 16 5 25 24 ÷5 ÷8 This can be done repeatedly until the numerator and denominator are

This can be done repeatedly until the numerator and denominator are the smallest possible numbers - the fraction is then said to be in its <u>simplest form.</u>

**Example 2** Simplify 
$$\frac{72}{84}$$
  $\frac{72}{84} = \frac{36}{42} = \frac{18}{21} = \frac{6}{7}$  (simplest form)

Calculating Fractions of a Quantity

To find a fraction of an amount :• Divide by the denominator (bottom number)• Multiply the answer by the numerator(top number)• You may sometimes get a whole number or a decimal answer**Example 1:** Find  $\frac{1}{5}$  of £150 $\frac{1}{5}$  of £150 = £150 ÷ 5 = £30 then £30x1= £30**Example 2:** Find  $\frac{3}{4}$  of 4848 ÷ 4 = 12 $50 3 \times 12 = 36$ Note again: Divide by the denominator (bottom number), then multiply the answer by the numerator (top number)

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S<sup>.</sup>

Numeracy Across St Anne's PERCENTAGES Percent means out of 100. A percentage can be converted to an equivalent fraction or decimal. Remember a decimal like 0.3 is the same as 0.30. Similarly with money, if you get an answer like £4.8 it means £4.80. To change a percentage to a To change a % to a fraction put it over 100. decimal we divide by 100. Eg 47% = <u>47</u> 100 Eg 62%=62÷100=0.62 36% means  $\frac{36^{L}}{100}$ which equals 36÷100 which equals 0.36 36% =  $\frac{36}{100}$  which can be simplified to  $\frac{9}{25}$  by dividing top and bottom by 4

### **Common Percentages**

Some percentages are used very frequently. It is useful to know these as fractions and decimals.

Percentage	Fraction	Decimal
1%	$\frac{1}{100}$	0.01
10%	$\frac{1}{10}$	0.1 same as 0.10
25%	$\frac{1}{4}$	0.25
50%	$\frac{1}{2}$	0.5 same as 0.50
75%	$\frac{3}{4}$	0.75
20%	$\frac{1}{5}$	0.2 same as 0.20

# PERCENTAGES USING MENTAL METHODS

There are many ways to calculate percentages of a quantity. Some of the common ways are shown below.



- Non- Calculator Methods
- Method 1 Using Equivalent Fractions

Example Find 25% of £640 (Remember 25% is one quarter)

25% of £640 = 
$$\frac{1}{4}$$
 of £640 = £640 ÷ 4 = £160

#### <u>Method 2</u>

- First find 1% of the quantity (by dividing by 100)
- Then multiply this answer by the percentage to get the required value

Example Find 9% of 200g 1% of 200g = 200g ÷ 100 = 2g

so 9% of 200g = 9 x 2g = 18g

#### Method 3 Using 10%

- First find 10% (by dividing by 10)
- Then multiply this answer by the combination of 10 to get the required value
   70% = 7x10% so

Example Find 70% of £35

70% = 7x10% so multiply by 7 after dividing by 10

imple Find 70% of £35

10% of £35 = 
$$\frac{1}{10}$$
 of £35 = £35 ÷ 10 = £3.50

so 70% of 
$$£35 = 7 \times £3.50 = £24.50$$

# PERCENTAGES BY CALCULATOR

#### **Calculator Method**

To find the percentage of a quantity using a calculator

- divide the percentage by 100
- then multiply this answer by the amount

Example 1 Find 23% of £15000

- 23% = 23÷100= 0.23
- so 23% of £15000 = 0.23 × £15000 = £3450



Equally we could do <u>Amount × Percentage</u> 100 So 23% of £15000 = <u>23 × 15000</u> = £3450 100

**Example 2** House prices increased by 19% over a one year period. What is the new value of a house which was valued at £236,000 at the start of the year?

19% = 0.19 so Increase = 0.19 x £236,000 = £44,840

Value at end of year = original value + increase = £236,000 + £44,840 = £280,840

The new value of the house is £280,840

- When increasing by a percentage we find the percentage of the amount then **ADD** this answer to the original number
- When decreasing by a percentage we find the percentage of the amount then **SUBTRACT** this answer from the original number

# EXPRESSING AN AMOUNT AS A PERCENTAGE

#### Expressing something as a percentage

To find a number as a percentage of another number:

- We make a fraction of both numbers
- Multiply this fraction by 100
- **Example 1** There are 30 pupils in Class 3M. 18 are girls. What percentage of Class 3M are girls?

 $\frac{18}{30} = 18 \div 30 = 0.6 \times 100 = 60\%$ 

Move the decimal point 2 places to the right (100 has 2 zeroes) 0.6 means 0.60

OR 
$$\frac{18}{30} \times 100\% = \frac{18 \times 100\%}{30} = \frac{1800}{30} = 60\%$$

60% of 3M are girls

**Example 2** James scored 36 out of 44 his biology test. What is his percentage mark?

Score =  $\frac{36}{44}$  = 36 ÷ 44 = 0.8181×100= 81.81% = 82% (nearest whole number)

OR 
$$\frac{36}{44} \times 100\% = \frac{36 \times 100\%}{44} = \frac{3600}{44} = 81.818..\% = 82\%$$

Example 3 In class 8J, 14 pupils had brown hair, 6 pupils had red hair, 3 had black hair and 2 had blonde hair. What percentage of the pupils had red hair?

> Total number of pupils = 14 + 6 + 3 + 2 = 256 out of 25 had red hair, so  $\frac{6}{25} = 6 \div 25 = 0.24$  0.24 × 100 = **24% had red hair**



# <u>RATIO</u>



When quantities are to be mixed together, the ratio, or proportion of each quantity is often given. The ratio can be used to calculate the amount of each quantity, or to share a total into parts.

# Writing Ratios



To make a fruit drink, 4 parts water is mixed with 1 part of orange squash. The ratio of water to squash is 4:1 (read as "4 to 1") The ratio of squash to water is 1:4.



Always read the question to ensure the ratio is written in the order given. If a bag has 2 yellow and 3 green balls then the ratio of yellow to green is 2:3 but green to yellow is 3:2

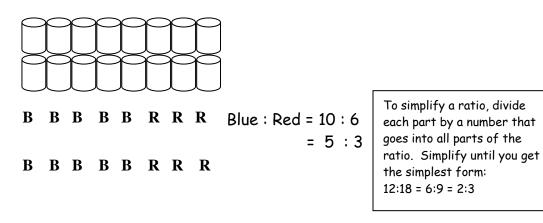
### Simplifying Ratios

Ratios can be simplified in much the same way as fractions.

### Example 1

Purple paint can be made by mixing 10 tins of blue paint with 6 tins of red. The ratio of blue to red can be written as 10 : 6

It can also be written as 5:3, as it is possible to split up the tins into 2 groups, each containing 5 tins of blue and 3 tins of red.

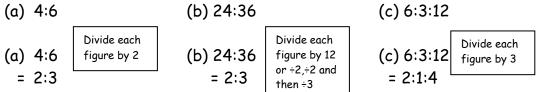


# SIMPLIFYING RATIOS

### Simplifying Ratios (continued)

#### Example 2

Simplify each ratio: To save time, divide by the biggest number possible, or divide in a number of smaller steps



#### Example 3

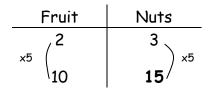
Concrete is made by mixing 30 kg of sand with 18 kg cement. Write the ratio of sand : cement in its simplest form

Sand : Cement = 30 : 18 divide by 2 = 15 : 9 divide by 3 = 5:3 simplest form

(Alternatively we could have divided by 6 to get the same answer)

### Using ratios

The ratio of fruit to nuts in a chocolate bar is 2 : 3. If a bar contains 10g of fruit, what weight of nuts will it contain?



So the chocolate bar will contain 15g of nuts.

# SHARING IN A GIVEN RATIO

#### Sharing in a given ratio Method:

• Add the ratio parts

- You can remember this as the ADaM (like the boy's name) ie Add then Divide then Multiply
- Divide the amount by this sum
- Multiply each amount of the ratio by this answer

#### <u>Example</u>

Betsy and Brian work in a pizza restaurant. Betsy worked for 5 hours and Brian worked for 3 hours. They decide to share out the total tip according to the hours they worked. If the total tips amount was £56, how much do they each get?

Betsy hours	: Brian hours gives the ratio as 5 : 3
Step 1	Add up the numbers to find the total number of parts
	5 + 3 = 8
Step 2	Divide the total by this number to find the value of each part
	56 ÷ 8 = 7
Step 3	Multiply this answer by each ratio amount
	5 x £7 = £35
	3 × £7 = £21
Step 4	Check that the total is correct
	£35 + £21 = £56 √
	Betsy received £35 and Brian received £21

# PROPORTION



Two quantities are said to be in direct proportion if, when one changes, the other changes in the same way

e.g. if one quantity doubles the other also doubles.

We can use proportion to solve problems.

It is often useful to make a table when solving problems involving proportion.

#### Example 1

A factory produces 1200 phones in 40 days. How many phones would they produce in 120 days?

Days	Phones
<sub>/</sub> 40	120Q
× <sup>3</sup> ( 120	<b>3600</b> ×3

The factory would produce 3600 phones in 120 days.

#### Example 2

5 adult tickets for the cinema cost £36.50. How much would 8 tickets cost?

	Tickets	Cost		
	5	£36.50		Find the cost
	1	£7.30	Working:	of 1 ticket
	8	£58.40		
	►	£7.30	£7.30	
The cost of 8 tick	ets is £58.4	5£36.50	₂ <b>× 8</b>	
				£58.40

# ROUNDING MONEY

All calculations of money need to be written down to <u>2 decimal places</u>. For example £6.8 on the calculator means £6.80.

For rounding we will use the rule of 'Five or more' which says that: 'look at the next digit after the position you want to round to - if this digit is 5 or more (eg 5, 6, 7, 8 or 9) then add 1 to the previous digit. If it is less than 5 then leave the previous digit as it is'

**Example 1** Round £3.268 to 2 decimal places

The second digit after the decimal point is a 6 - check the next digit (the third number after the decimal point) which is an 8, as it's more than 5 we add 1 to 6 to make it 7.

£3.268 = <u>£3.27 to 2 decimal places</u>

**Example 2** Round £13.432 to 2 decimal places

The second digit after the decimal point is a 3 - check the next digit (the third number after the decimal point) which is a 2 so as it's less than 5 we leave 3 as it is

£13.432 = £13.43 to 2 decimal places

### CALCULATIONS WITH MONEY

**Problem**: You are working at a cake stall. There are two different ways for you to be paid. Either you can be paid PER HOUR, or you can receive a PERCENTAGE of the total profits.

**OPTION 1**: You work for three hours. The wage that they pay is  $\pounds 5$  per hour.

**OPTION 2**: The total profits are £180. They offer you 10%. Which option would you choose and why?



**Option 1** £5.00 per hour.

Three hours in total.

5 x 3 = 15

So you would be paid £15.

# Option 2

10% is the same as splitting 100% into 10 pieces:

10%+10%+10%+10%+10%+10%+10%+10%+10%=100%

#### Therefore, 10% is the same as dividing by 10.

The Total Profits: £180

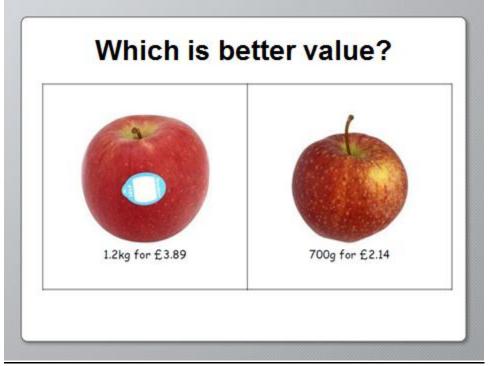
If we split that into 10 pieces (divide by 10), we will find out what 10% of 180 is.

£180 ÷ 10 = £18.

So you would be paid £18.

So OPTION 2 will give you £3 more than OPTION 1

#### BEST BUYS

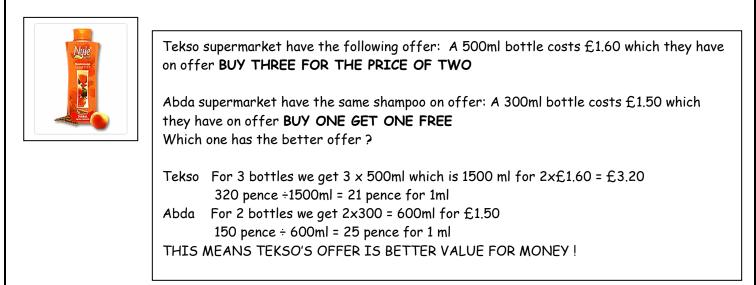


FACT: 1 kg = 1000g and £1 = 100 pence

Find the cost of 1g for each

1200g = 389 pence so  $1g = 389 \div 1200$ we get 1g = 0.32 pence700g = 214 pence so  $1g = 214 \div 700$ we get 1g = 0.31 pence

So 700g for £2.14 is better value for money



# SALES PRICES & OFFERS

Percentage Discounts							
152	<ul> <li>To find the sale price of an item:</li> <li>We find the percentage of the amount</li> <li>Subtract this answer from the original amount</li> </ul>						
Method 1	Using Equivalent Fractions						
Example	<b>Example</b> A Shirt usually costs £50 but is discounted by 25% in the sale. How much does it cost in the sale?						
The shirt h	as 25% of its value taken away from its original price:						
$25\% \text{ of } \pounds 50 = \frac{1}{4} \text{ of } \pounds 50 = \pounds 50 \div 4 = \pounds 12.50$ Take this away from the original price: $\pounds 50.00 - \pounds 12.50 = \frac{\pounds 37.50}{\pounds 37.50}$ To divide by 4 we divide by 2 then divide that answer by 2							
<b>Method 2</b> Using 1% method In this method, first find 1% of the quantity (by dividing by 100), then multiply to give the required value.							
<b>Example</b> A bicycle usually costs £300 but is discounted by 20% in the sale. How much does it cost in the sale?							
	1% of £ 300 = $\frac{1}{100}$ of £ 300 = £ 3						
so 20% of £ 300 = 20 x £ 3 = £ 60 Take this away from the original price: £ 200- £ 60 = <u>£ 140</u>							

SALE PRICES AND OFFERS (continued) Method 3 Using the 10% method Firstly find 10% by dividing the amount by 10 Multiply this answer by the combination of 10 For example to find 40% we divide by 10 then multiply the answer by 4 because  $40\% = 4 \times 10\%$ A pair of football boots are reduced by 30 % in a sale. If their Example original price was £90, calculate the sale price: 10% of £90 =  $\frac{1}{10}$  of £90= £90÷ 10 = £9 30% of £90 =  $3 \times £9 = £27$ Take this away from the original price: £.90 - £.27 = £ 63 Percentage Discounts: Calculator Method 52 Find the percentage of the amount by • Divide the % by 100 then multiply by the amount Subtract this answer from the original amount **Example 1** A car usually costs £15000 but is reduced by 23% as part of a promotion for this week only. Calculate the cost of the car now. 23% = 0.23÷100=0.23 so 23% of £15000 = 0.23 x £15000 = £3450 Take this away from the original price: - £ 3450 = £ 11 550 £ 15 000

#### CALCULATING WITH FORMULAE



To find a value of a **variable** (this is a letter whose value changes) in a given formula:

- Substitute the numbers we are given into the formula
- Use BIDMAS to calculate the answer

#### <u>Example 1</u>

Given the formula V=U + AT what is the value of V when U=3, A=2 and T=7

•	Write the formula	V = U + AT
•	Substitute in numbers	V = 3 + 2 × 7
٠	Use BIDMAS ( x then +)	V= 3 + 14
٠	Write down the answer	V= 17

#### <u>Example 2</u>

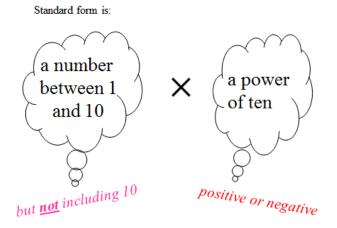
Given the formula Y=MX + C what is the value of C when Y=15, M=2 and X=4

<ul> <li>Write the formula</li> </ul>	Y = MX + C
Substitute in numbers	15 = 2×4 + <i>C</i>
• Use BIDMAS	15 = 8 + <i>C</i>
<ul> <li>Solve for C</li> </ul>	15 - 8 = <i>C</i>

- (sign of term changes when you take it over the equals sign) REMEMBER THIS AS : "CHANGE SIDE, CHANGE SIGN"
- Write down the answer C = 7

Note: when calculating this we got 7 = C which is the same if we turn it around as C = 7

#### STANDARD FORM



Example The Jurassic Age began 199600000 years ago.

Write this in standard form.

1<mark>.</mark>996 x 10<sup>8</sup>

The number we have is 199600000 - the decimal point is always at the end of a whole number. We have to move the decimal point until we get a number between 1 and 10. We had to move it 8 times so the power is 8 ! **Moving left gives a positive power** 

#### Example

A DNA chain is approximately 0.0000022 mm in width.

Write this in standard form.

MM MM

0.0000022

2.2 x 10<sup>-6</sup>



The number we have is 0.0000022 - we have to move the decimal point to the right this time to get a number between 1 and 10. **Moving to the right gives a negative power** As we had to move 6 times the power is -6

# TIME NOTATION



Time may be expressed in 12 or 24 hour notation. 12 hour notation has am or pm written at the end. 24 hour notation does not ! eg 13:40 is 1.40pm

12-hour clock

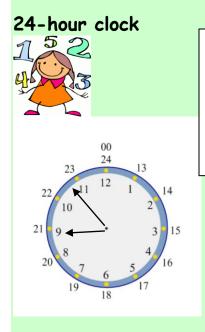
Time can be displayed on a clock face, or digital clock.



These clocks both show fifteen minutes past five, or guarter past five.

When writing times in 12 hour clock, we need to add a.m. or p.m. after the time.

a.m. is used for times between midnight and 12 noon (morning) p.m. is used for times between 12 noon and midnight (afternoon / evening).



For the 24 hour clock system the numbers are between					
00 and 24. Midnight is 0:00 or 24:00.					
After 12 noon the hours are numbered as follows:					
1.00pm is 13:00					
2.00pm is 14:00 (The colon : may not appear)					
3.00pm is 15:00 etc (You may see h written as well)					
Other ways you may see 24 hour clock times are					
1420h which is the same as 14:20h (2.30 pm)					

#### Examples

6.35 am	→ 06:35 h
3.40 pm	→ 15:40 h
11.45 am	<b>→</b> 11:45 h
03:50 h	► 3.50 am
20:45 h	<b>⊾</b> 8.45 pm

# TIME PERIODS



You need to know the time facts as follows: 1 minute = 60 secs, 1 hour = 60 mins, 1 day = 24 hours 1 week = 7 days, 1 year = 52 weeks not 48!!

Time Facts In 1 year, there are:

365 days (366 in a leap year) 52 weeks 12 months

Also remember that 1 century = 100 years

The number of days in each month can be remembered using the rhyme: "30 days hath September, April, June and November, All the rest have 31, Except February alone, Which has 28 days clear, And 29 in each leap year."

• To change a 24 hour time into a 12 hour time we SUBTRACT 12 from the hours part if the hours are more than 12 which means it's after 12 noon

Example:  $18:40h \rightarrow subtract 12 \text{ from } 18$ 18 - 12 = 6 so the time is 6.40 pm

Example: 06:55→as the hours part is less than 12 then this is before midday (noon) so no need to subtract. This time is 6.55am in the morning

- Remember the equivalent notation for the 24 hour clock can be written in different ways:
- 16:30 or 16:30h is the same as 1630 or 1630h which is also the same as 16 30 or 16 30 hours (h or hours are the same !)

### INTERPRETING TIMETABLES

Destination	Time								
Thurso Business Park	0645	0745	0905	1005	1105	1205	1305	1405	1505
<b>Olrig Street</b> Job Centre	0650	0750	0910	1010	1110	1210	1310	1410	1510
Halkirk Sinclair Street	0705	0805	0925	1025	1125	1225	1325	1425	1525
Watten Post Office	0718	0818	0938	1038	1138	1238	1338	1438	1538
<b>Haster</b> Fountain Cottages	0725	0825	0945	1045	1145	1245	1345	1445	1545
Wick Somerfield bus terminal	0730	0830	0950	1050	1150	1250	1350	1450	1550
Wick Business park	0735	0835	0955	1055	1155	1255	1355	1455	1555
Wick Tesco Store	0736	0836	0956	1056	1156	1256	1356	1456	1556
Wick Airport Terminal	0741	0841	1001	1101	1201	1301	1301	1401	1601

#### Examples of Questions:

a) I want to be at Wick Airport by 2.30pm. What time must I catch the bus at Olrig Street Job Centre?

2.30pm is shown as 1430 h on the timetable The most suitable bus arrives at Wick Airport at 1401 This leaves Olrig Street Job Centre at <u>1410 h</u>

b) The 0745 bus from Thurso Business Park is running 6 minutes late. What time does it reach Wick Tesco Store?

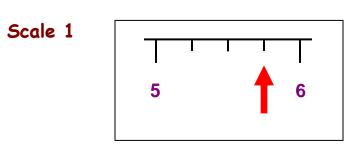
Add 6 minutes to the arrival time at Wick Tesco Store This is 0836 h. <u>It arrives at **0842** h</u>

c) How long does the first bus journey from Halkirk to Wick Business Park take?

The bus leaves Halkirk at 0705 h and arrives at Wick Business Park at 0735 h. The journey time is <u>30 minutes.</u>

### READING SCALES





In this scale the difference between 5 and 6 is 1, and the space has been divided into 4, so each division represents  $1 \div 4 = 0.25$ .

The arrow is pointing to 5 + 0.25 + 0.25 + 0.25 = 5.75

### Scale 2 - a speedometer



The difference between 50 and 60 is 10 and the space has been divided into 2, so each division represents  $10 \div 2 = 5$ . The arrow is pointing to 50 + 5 = 55

So the Method is:

- SUBTRACT THE NUMBERS BETWEEN THE READINGS REQUIRED
- DIVIDE THE ANSWER YOU GET BY THE NUMBER OF DIVISIONS BETWEEN BOTH NUMBERS

### CONVERTING UNITS

The table shows some of the most common equivalences between different METRIC units of measure. Make sure you know these **conversions**. Metric units are the modern day units.

Length	Weight	Capacity
	1 tonne = 1000kg	
1 km = 1000m	1kg = 1000g	
1m = 100cm = 1000mm	1g = 1000mg	1l = 100cl = 1000ml
1cm = 10mm		1cl = 10ml

### METRIC & IMPERIAL UNITS

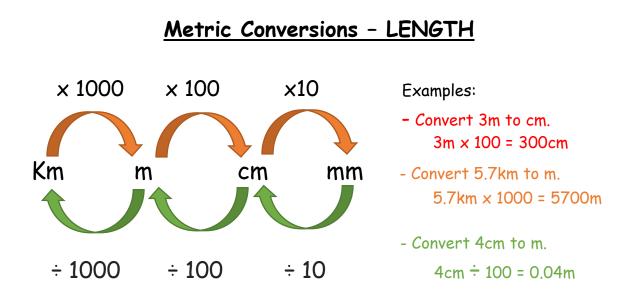
Imperial measures are old-fashioned units of measure. These days we have mostly replaced them with metric units, but despite our efforts to 'turn metric', we still use many imperial units in our everyday lives. It is therefore important that we are able to calculate rough equivalents between metric and imperial units.

Here are some conversions that you will need to know:

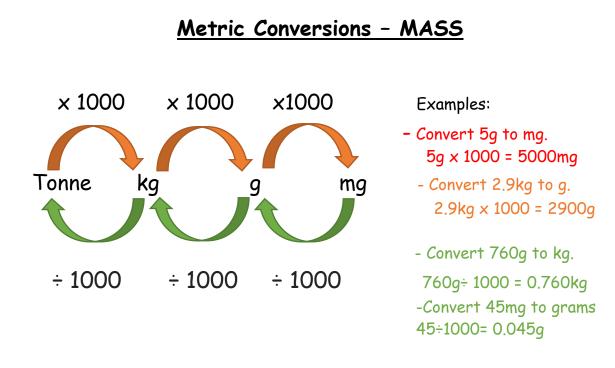
inch is about 2.5cm
 foot is about 30cm
 gallon is about 4.5 litres
 1kg is about 2.2 pounds
 litre is about 1.75 pints
 8km is about 5 miles

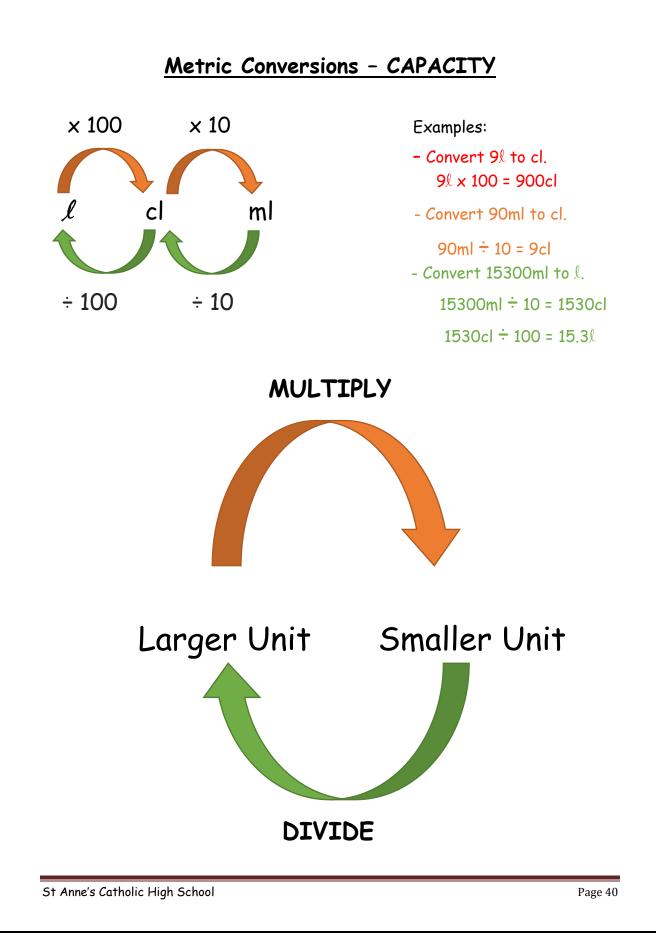
(1km is about 0.625 miles and 1 mile is about 1.6 km)

mm is millimetres cm is centimetres m is metres km is kilometres	g is grams kg is kilograms	ml is millilitres cl is centilitres ℓ is litres
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**Remember:** To convert from a larger unit to a smaller one, **multiply**. For example to change from **kilometres** to **metres** we **MULTIPLY** To convert from a smaller unit to a larger one, **divide**. For example to change to from **centimetres** to **metres** we **DIVIDE** 





# SCALE RATIOS



Ratios are used in everyday life and can help you work out problems involving scale drawings and reading maps.

In a scale drawing, all dimensions have been reduced by the same proportion.

**Example** A model boat is made to a scale of **1:20** (read as 1 to 20) meaning 1cm measured on the model is 20cm on the actual boat.

a) If the 1:20 model boat is 15cm wide, how wide is the actual boat?b) If the boat has a mast of height 4m, how high is the mast on the model?

The scale is **1:20**. This means that every cm on the model is equivalent to 20cm on the boat.

a) 1cm on the model = 20cm on the boat, so:
15cm × 20 = 300cm.
15cm on the model = **300cm** (which is 300÷100 = 3m on the boat)

Remember: Multiply to get the actual measurement

b) 20cm on the boat = 1cm on the model

Remember 1 metre = 100 centimetres so mast height on real boat ÷ 20 = mast height on model 4m is 4×100cm=400cm on the boat = 400cm ÷ 20 = 20cm on the model

Remember: Divide to get back down to the scale measurement

# MAP SCALES

A map scale is given as 1:50000.

a) What is the actual distance in kilometres between Town A and Town B if the measurement on the map is 3 cm?

The scale of 1:50000 means that 1 cm on the map represents 50000 cm in reality

Therefore 3cm it three times as much  $\rightarrow$  3 x 50000 = 150000 cm

150000 cm = 150000 ÷ 100 metres = 1500 metres

1500 metres = 1500 ÷ 1000 km = 1.5 km between Town A and Town B

b) If the actual measurement between Town C and Town D is 2.7 km, what distance in cm would this be on the map?

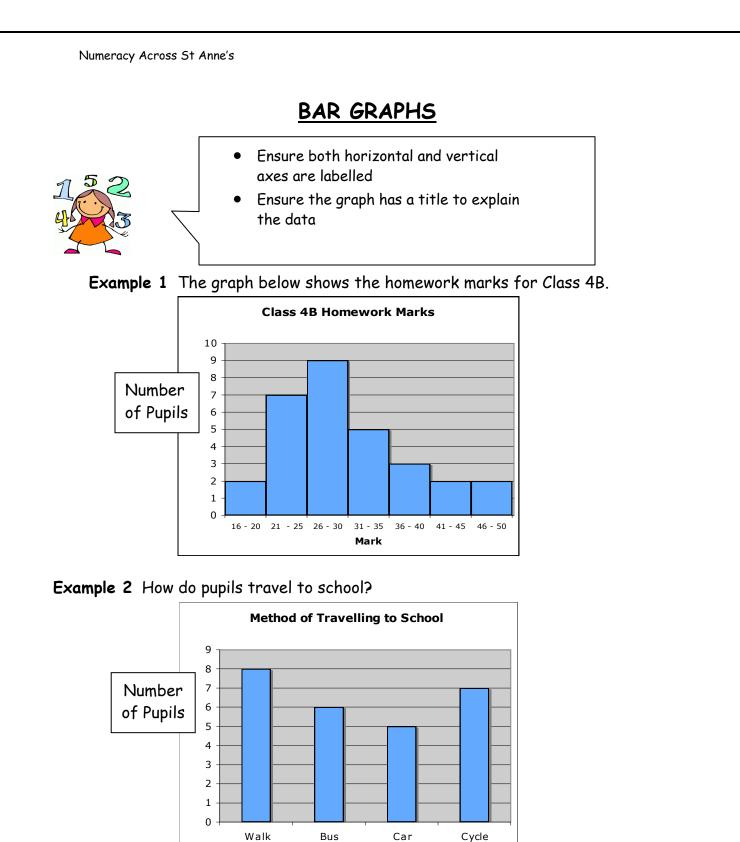
2.7 km= 2.7 × 1000m = 2700 metres

2700 x 100 cm = 270000 cm and every 1 cm equals 50000cm so we need to see how many of these we have  $\rightarrow$  therefore we divide

270000 ÷ 50000 = 5.4 cm on the map between Town C and Town D

- To scale up to the actual distance we MULTIPLY
- To scale down to the map distance we DIVIDE
- Ensure your units are in the right form before you multiply or divide





When the horizontal axis shows categories (worded data like colour, type of car etc) rather than grouped intervals, it is common practice to leave gaps between the bars.

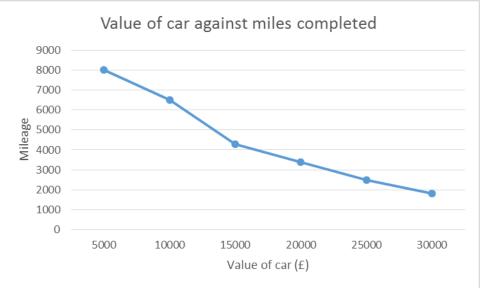
Method

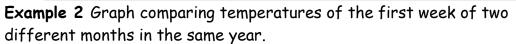
## LINE GRAPHS

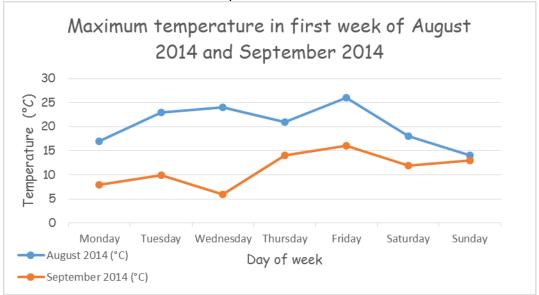
Line graphs consist of a series of points which are plotted, then joined by a line. All graphs should have a title, and each axis must be labelled. The trend of a graph is a general description of it.



**Example 1** The graph below shows a car's value depreciating as it mileage increases. (Depreciate means to go down in value)







## SCATTER GRAPHS

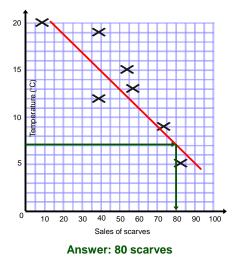


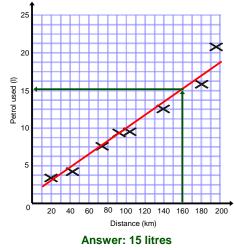
- A scatter diagram is used to display the relationship between two sets of data
  - This relationship is called the 'correlation'
- A straight line called a 'line of best fit' is used to estimate data

#### Scatter Graphs • A line of best fit roughly follows the pattern of the points • It does NOT have to go through any points or start on the axes Positive correlation example: As the temperature increases the number of ice-creams sold increases Negative correlation: As the age of a car increases, the value of it decreases **Positive Correlation** Negative Correlation No Correlation $\rightarrow$ As one value $\rightarrow$ There is no pattern $\rightarrow$ As one value increases, the other increases, the other in the data (and increases decreases therefore no line of best fit ... )

Estimate, using your graph, how many scarves the shop would sell when the temperature was 7°C.

Estimate, using your graph, how many litres of petrol the car would use on a journey of 160km.





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## PIE CHARTS

## Drawing Pie Charts



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METHOD

Find the total of your data

Put each amount over the total

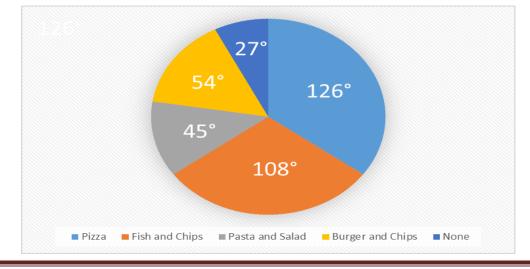
• Multiply by 360°

- -

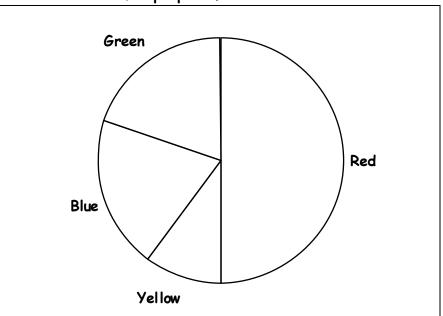
**Example:** In a survey about eating, a group of people were asked what their favourite food was. Their answers are given in the table below. Draw a pie chart to illustrate the information.

Favourite food	Number of people
Pizza	28
Fish and Chips	24
Pasta and Salad	10
Burger and Chips	12
None	6

$$\begin{aligned} \text{Fish \& Chips} &= \frac{28}{80} \rightarrow \frac{28}{80} \times 360^\circ = 126^\circ \\ \text{Fish \& Chips} &= \frac{24}{80} \rightarrow \frac{24}{80} \times 360^\circ = 108^\circ \\ \text{Pasta \& Salad} &= \frac{10}{80} \rightarrow \frac{10}{80} \times 360^\circ = 45^\circ \\ \text{Burger \& Chips} &= \frac{12}{80} \rightarrow \frac{12}{80} \times 360^\circ = 54^\circ \\ \text{None} &= \frac{6}{80} \rightarrow \frac{6}{80} \times 360^\circ = 27^\circ \end{aligned}$$



### INTERPRETING PIE CHARTS



$\sim$		_	_
<b>9()</b>	neonle's	s favourite	colour
/ 🗸	people s		COIOUI

Favourite colour	Degrees	People
Red	180 <sup>0</sup>	
Yellow	36 <sup>0</sup>	
Blue	72 <sup>0</sup>	
Green	72 <sup>0</sup>	
Total		90

Method: <u>Degrees in section</u> × Total 360°

TOTAL = 90 people RED =  $\frac{180^{\circ}}{360^{\circ}} \times 90 = 45$  people  $YELLOW = \frac{36^{\circ}}{360^{\circ}} \times 90 = 9$  people BLUE =  $\frac{72^{\circ}}{360^{\circ}} \times 90 = 18$  people so GREEN is also 18 people

# AVERAGES



- There are 3 different types of averages
  - Mean
  - Median
  - Mode.

### <u>Mean</u>

The mean is found by adding all the numbers together and dividing by the number of values.

### <u>Median</u>

The median is the middle value when all the data is written in numerical order (if there are two middle values, the median is found by adding the two middle numbers then dividing by 2).

### <u>Mode</u>

The mode is the value that occurs most often. If there is more than one mode - we call these the **modal values** 

**Range** This gives us an idea about the spread of the data

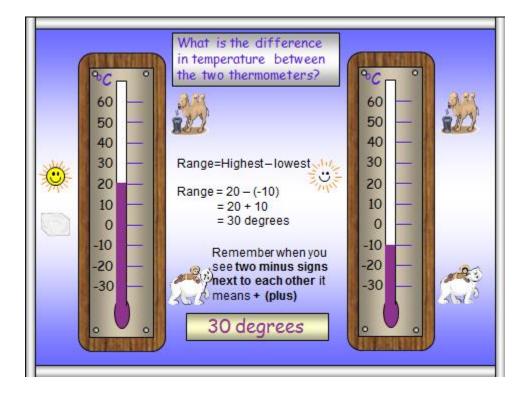
Range = Highest value - Lowest value

**Example** Mary got the following scores in a bowling competition

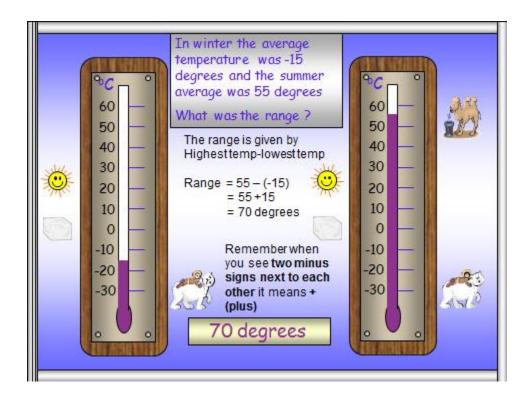
6, 5, 8, 4, 9, 9, 7, 10, 8, 5, 8, 2

Mean = <u>6+5+8+4+9+9+7+10+8+5+8+2</u> 12 = <u>81</u> 12 Mean = 6.8 to 1 decimal place Ordered values: 2, 4, 5, 5, 6, <u>7, 8,</u> 8, 8, 9, 9, 10 Median = (7+8 = 15 so 15+2=7.5) Median = 7.5

8 is the most frequent mark, so **Mode = 8** Range = 10 - 2 = 8



#### RANGE FROM THERMOMETER READINGS



## REARRANGING EQUATIONS

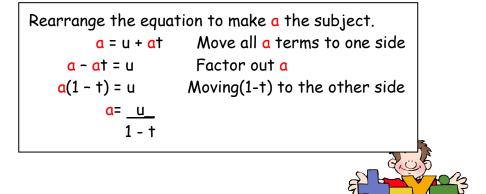
### REARRANGING EQUATIONS

"The 'subject' is the letter at the front of the equation" Change the subject in the following to make y the subject

y + x - 3 = 0 so moving x and 3 to the other side gives y = 3 - x When we move letters or numbers to the other side they change sign **REMEMBER:** CHANGE SIDE, CHANGE SIGN !

Rearrange the formula v = u + at to make a the subject.

v = u + at Move u first v - u = at Move t (by dividing) v - u = at Rearranging is a bit like **solving** to find the letter you want to make the **subject**.



Remember:

- Firstly decide what letter needs to be the subject
- Move all terms that are not needed to one side remember to **change the sign** when taking terms over the equals sign (if they are being added or subtracted only !)
- The sign does not change for multiplying and dividing terms!
   Eg in the second example we divide by t not -t & in third example we divide by (1-t) not -(1 t)

#### PLOTTING COORDINATES



- The x axis is the horizontal line across
- The y axis is the vertical line up

The **ORIGIN** is the point at the centre.

When plotting or reading coordinates we always:

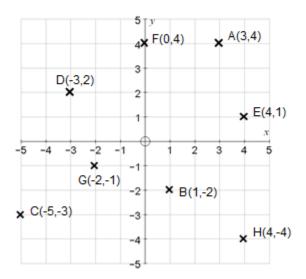
1.Start at the origin

2.Go across the x axis first (the horizontal one) - right if positive or left if negative. You can remember this as 'along the corridor'

3. Then **go up (or down) the y axis** ( the vertical one) - up if positive or down if negative. You can remember this as 'up/down the stairs'

#### 'ALONG THE CORRIDOR AND UP/DOWN THE STAIRS'

### Coordinates in all 4 quadrants



## MATHEMATICAL KEYWORDS

Addition(+)	To combine 2 or more numbers together. The answer is called the SUM or TOTAL	
a.m.	(meaning ante meridiem (Latin)) This refers to any time in the morning between midnight and 12 noon. Used in 12 hour clock notation.	
Approximate	An estimated answer	
Annual	Taking place yearly	
Bar Chart	This is a graph showing the frequency of data using bars	
Bearing	This is a clockwise angle measured from the North line (a 3 digit number)	
Brackets	Used around calculations to show what needs to be calculated first	
Co-interior	Angles inside parallel lines which always add to 180°	
angles		
Coefficient	This is the number in front of a term eg 3x the coefficient of x is 3, $4x^2$ the coefficient of $x^2$ is 4	
Congruent	2D shapes that are exactly the same shape and size	
Cube	Any number or algebraic term to the power 3 eg $4^3$ or $a^3$	
Cuboid	Rectangular box eg like a shoe box or matchbox	
Continuous	Data that can take any value (within a range) Example: People's heights	
Data	could be any value (within the range of human heights)	
Denominator	This is the bottom number in a fraction	
Discrete Data	Data that can only take certain values. For example: the number of	
	students in a class (you can't have half a student).	
Difference	This is the answer when you subtract 2 numbers	
Division	Sharing a number into equal parts. The answer is called the QUOTIENT	
Equation	A statement that the values of two mathematical expressions are equal (indicated by the sign =).	
Estimate	To make an approximation or rough answer to a calculation	
Expand	To multiply out a bracket eq $3(a + 2) = 3a + 6$	
Factor	A number which divides exactly into another number	
	eg factors of 6 are 1,2,3 and 6	
Factorise	Used in Algebra to put brackets back in eg 6a + 9b = 3(2a + 3b)	
Frequency	How often something happens eg how many red cars were seen	
Greater than	In Maths greater than is shown by the symbol >	
Mean	The average of a data set. Add numbers then divide by how many numbers	
Meun	there are	
Median	Another type of average. Order the data set then find the middle number	
Mode	Another type of average. This is the most frequent number(s)	
Multiple	This is the times table of the number eg multiples of 3 are 3,6,9,12,15,18	
Multiply	To combine an amount a particular number of times. The answer is called the PRODUCT. Eg The product of 2x4 is 8	
Negative	This is a number less than zero. Shown by a minus sign in the front	
Number	Eg -6 and -3.7	
Numerator	This is the top number in a fraction	

Operation	Operations are addition, subtraction, multiplication and division	
Parallel lines	Straight lines that are always the same distance apart and never meet	
Percentage	Means per hundred eg 30% means 30÷100	
Perimeter	This is the distance around a shape found by adding all the sides	
Perpendicular	Straight lines that are at right angles to each other	
Place value	The value of a digit which depends on its place in the number. For example,	
	356.8 the 5 has a place value of 50, 2389 the 3 has a place value of 300	
p.m.	(meaning post meridiem(Latin)). Any time between 12 noon and midnight	
Polygon	A side with many shapes eg pentagon (5 sides), hexagon (6 sides)	
Prime factor	r This is a factor of a number that is prime eg prime factors of 12 are 2 and	
	3 also prime factors of 30 are 2, 3 and 5	
Prime Number	A number with only 2 factors – the number itself and 1	
	Note: 1 is <b>not</b> considered prime as it only has 1 factor and 2 is the only	
	even prime number	
Range	The difference between two sets of data.	
	Range = Highest Value - Lowest Value	
Ratio	This is way to express the sizes of quantities eg ratio of girls to boys in	
	form 6B is 15:13 Shown by using a colon between the numbers	
Rhombus	A four sided shape (quadrilateral) which has:	
	All equal sides	
	Opposite sides parallel	
Trapezium	A four sided shape (quadrilateral) which has only <b>one</b> pair of parallel sides	